CE 3372 WATER SYSTEMS DESIGN LESSON 12: OPEN CHANNEL FLOW (GRADUALLY VARIED FLOW) FALL 2020

FLOW IN OPEN CONDUITS

- Gradually Varied Flow Hydraulics
 - Principles
 - Resistance Equations
 - Specific Energy
 - Subcritical, critical, supercritical and normal flow.

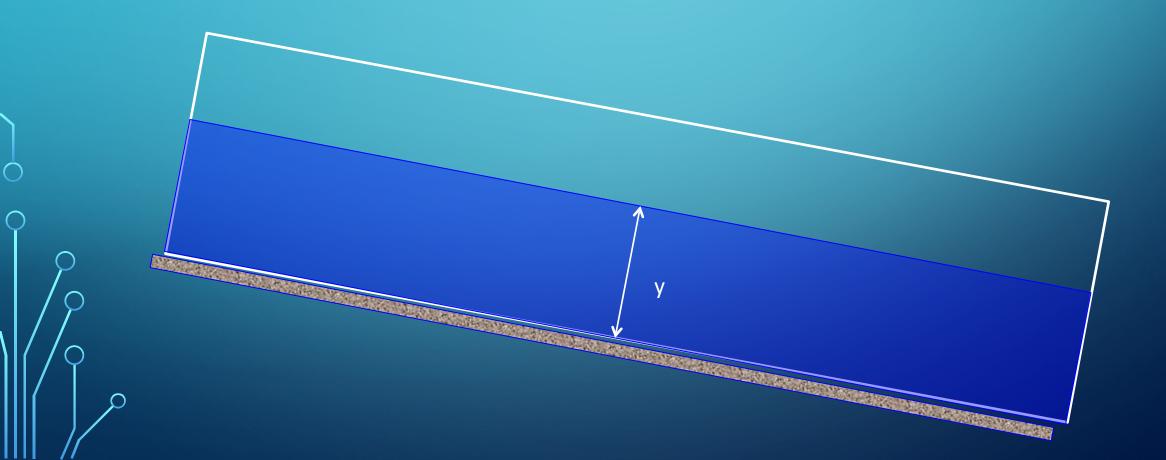
DESCRIPTION OF FLOW

- Open channels are conduits whose upper boundary of flow is the liquid surface.
- Storm sewers and sanitary sewers are typically designed to operate as open channels.
- The relevant hydraulic principles are the concept of friction, gravitational, and pressure forces.

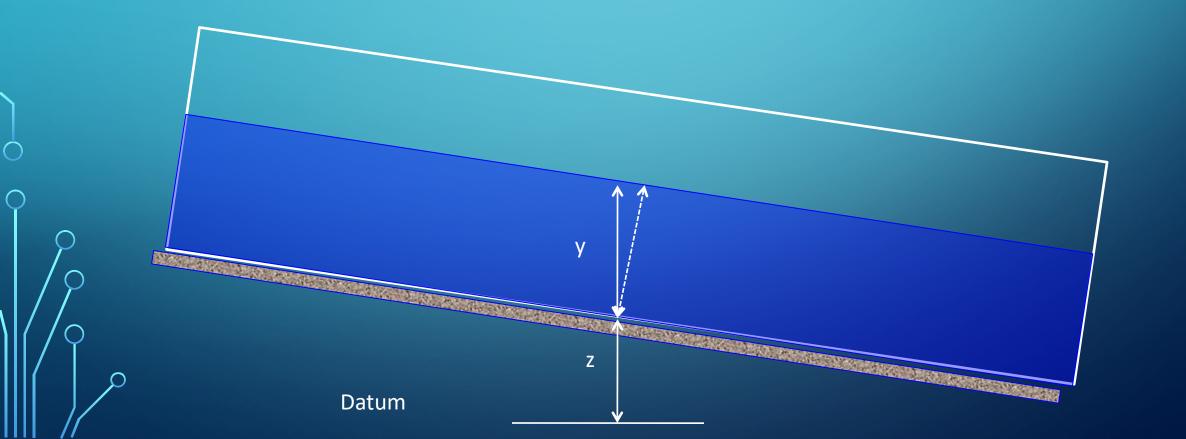
DESCRIPTION OF FLOW

- For a given discharge, Q, the flow at any section can be described by the flow depth, cross section area, elevation, and mean section velocity.
- The flow-depth relationship is non-unique, and knowledge of the flow type is relevant.

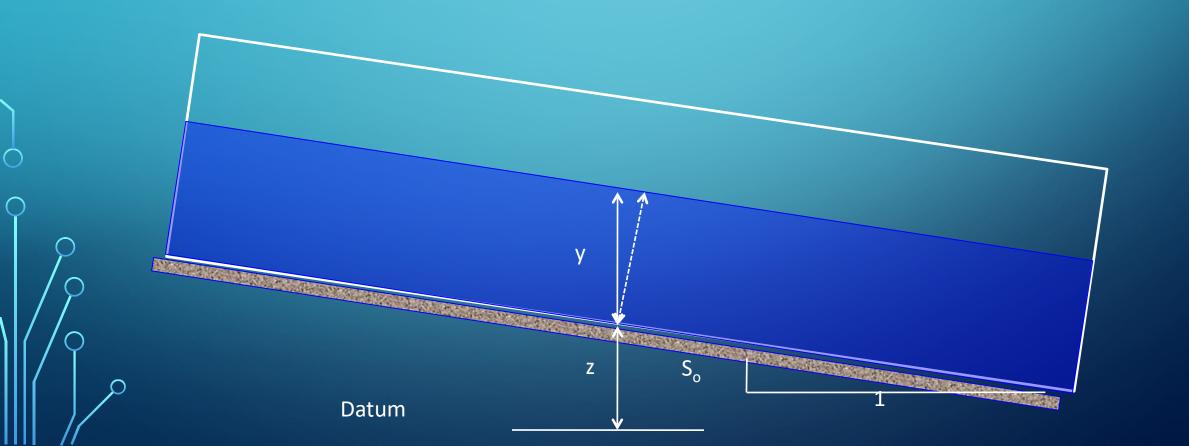
Flow depth is the depth of flow at a station (section) measured from the channel bottom.



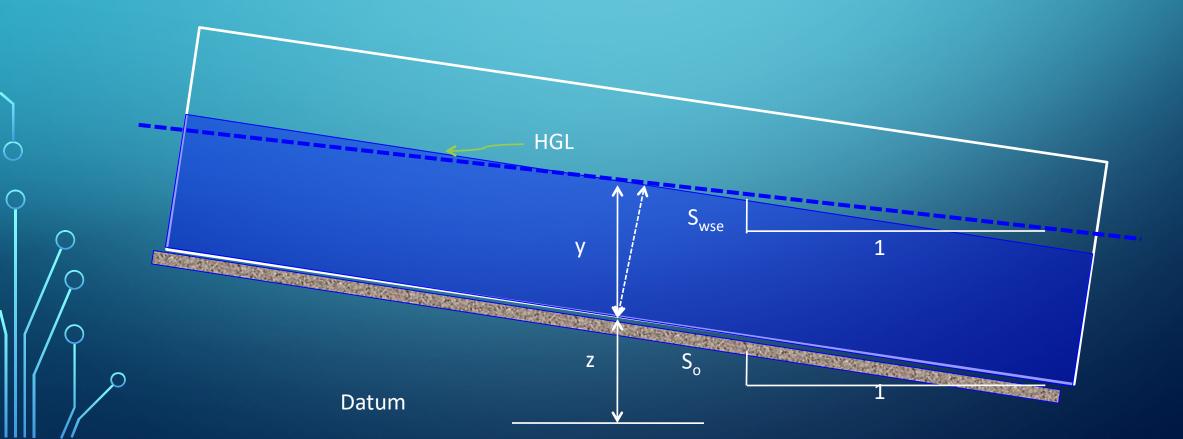
• Elevation of the channel bottom is the elevation at a station (section) measured from a reference datum (typically MSL).



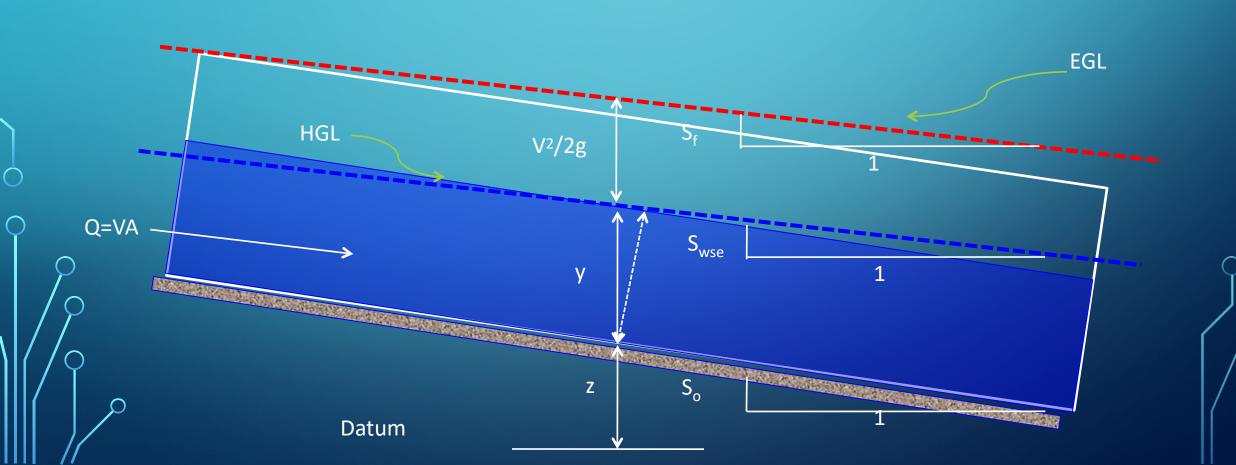
Slope of the channel bottom is called the topographic slope (or channel slope).



Slope of the water surface is the slope of the HGL, or slope of WSE (water surface elevation).



Slope of the energy grade line (EGL) is called the energy or friction slope.



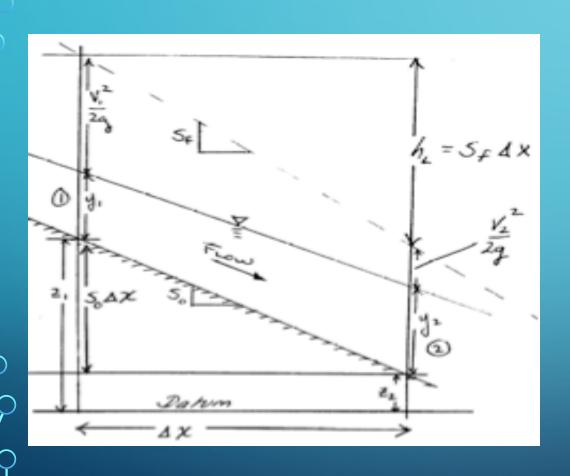
- Like closed conduits, the various terms are part of mass, momentum, and energy balances.
- Unlike closed conduits, geometry is flow dependent, and the pressure term is replaced with flow depth.

- Open channel pressure head: y
- Open channel velocity head: V²/2g (or Q²/2gA²)
- Open channel elevation head: z
- Open channel total head: h=y+z+V²/2g
- Channel slope: $S_0 = (z_1 z_2)/L$
 - Typically positive in the down-gradient direction.
- Friction slope: $S_f = (h_1 h_2)/L$

UNIFORM FLOW

- Uniform flow (normal flow; pg 104) is flow in a channel where the depth does not vary along the channel.
- In uniform flow the slope of the water surface would be expected to be the same as the slope of the bottom surface.

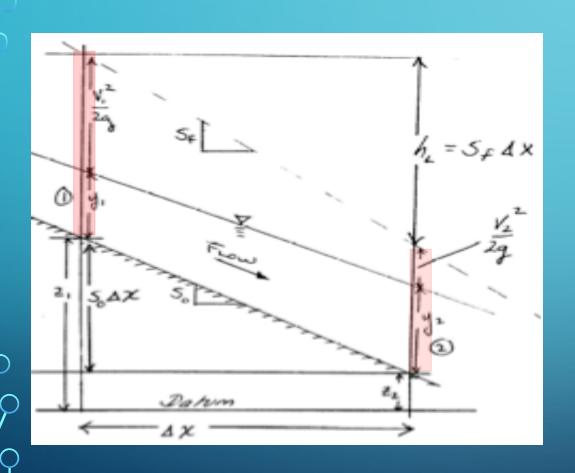
UNIFORM FLOW



- Uniform flow would occur when the two flow depths y1 and y2 are equal.
- In that situation:
 - the velocity terms would also be equal.
 - the friction slope would be the same as the bottom slope.

Sketch of gradually varied flow.

- Gradually varied flow means that the change in flow depth moving upstream or downstream is gradual (i.e. NOT A WATERFALL!).
 - The water surface is the hydraulic grade line (HGL).
 - The energy surface is the energy grade line (EGL).



 Energy equation has two components, a specific energy and the elevation energy.

Energy Equation from
$$0 \rightarrow 0$$

$$\frac{\sqrt{2}}{\sqrt{2}} + y_1 + z_1 = \frac{\sqrt{2}}{2g} + y_2 + z_2 + h_2$$

$$= \frac{\sqrt{2}}{2g} + y_1 + z_2 = \frac{\sqrt{2}}{2g} + y_2 + z_2 + h_2$$

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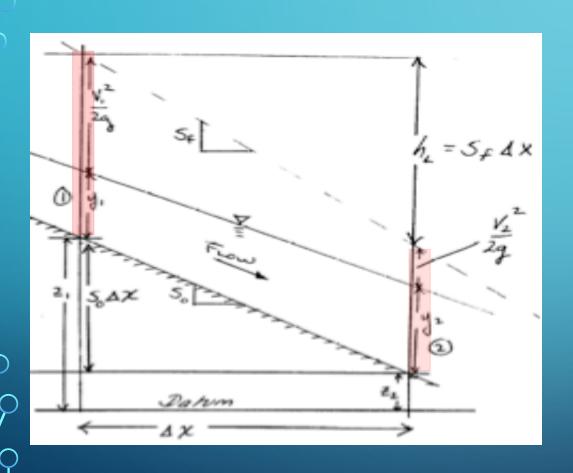
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$$= \frac{\sqrt{2}}{2g} + y_1 + y_2 + z_2$$

Sketch of gradually varied flow.



• Energy equation has two components, a specific energy and the elevation energy.

$$E_{1} + (E_{1} - E_{2}) = E_{2} + h_{L}$$

$$= S_{0} \Delta x$$

$$= S_{0} \Delta x$$

$$S_{F} \Delta x$$

$$S_{F} \Delta x$$

$$S_{F} \Delta x$$

Sketch of gradually varied flow.

Energy equation is used to relate flow, geometry and water surface elevation (in GVF)

$$E_1 + S_0 \Delta x = E_2 + S_f \Delta x$$

 The left hand side incorporating channel slope relates to the right hand side incorporating friction slope.

Rearrange a bit

$$S_0 - S_f = \frac{E_2 - E_1}{\Delta x}$$

• In the limit as the spatial dimension vanishes the result is.

$$S_0 - S_f = \frac{dE}{dx}$$

Energy Gradient:

$$S_0 - S_f = \frac{dE}{dx} = \frac{dE}{dy} \frac{dy}{dx}$$

- Depth-Area-Energy
 - (From pp 119-123; considerable algebra is hidden)

$$\frac{dE}{dy} = 1 - \frac{Q^2}{gA^3} \frac{dA}{dy} = 1 - Fr^2$$

Make the substitution:

$$S_0 - S_f = (1 - Fr^2) \frac{\partial y}{\partial x}$$

Rearrange

Variation of
Water Surface Elevation

$$\begin{cases} dy \\ dx \end{cases} = \frac{S_0 - S_f}{1 - Fr^2}$$

Discharge and Section Geometry

Discharge and Section Geometry

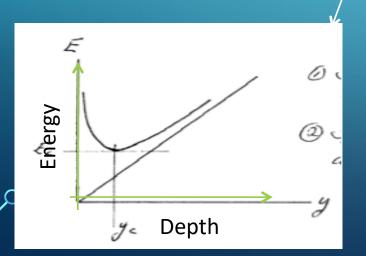
- Basic equation of gradually varied flow
 - It relates slope of the hydraulic grade line to slope of the energy grade line and slope of the bottom grade line.

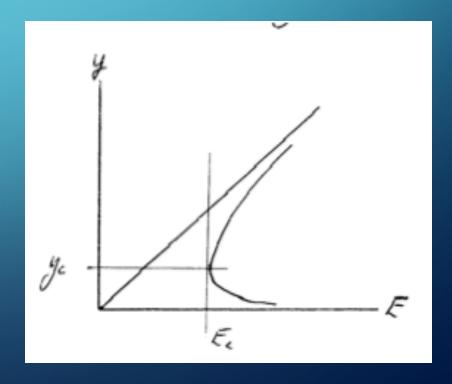
$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

 This equation is integrated to find shape of water surface (and hence how full a sewer will become)

Before getting to water surface profiles, critical flow/depth needs to be defined

- Specific energy:
 - Function of depth.
 - Function of discharge.
 - Has a minimum at y_c.





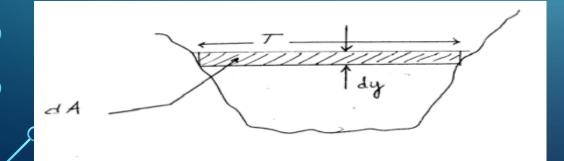
CRITICAL FLOW

Has a minimum at y_c.

Necessary and sufficient condition for a minimum (gradient must vanish)

$$\frac{dE}{dy} = 1 - \frac{Q^2}{gA^3} \frac{dA}{dy}$$

Variation of energy with respect to depth; Discharge "form"



Depth-Area-Topwidth relationship

CRITICAL FLOW

Has a minimum at y_c.

$$\frac{dE}{dy} = 1 - \frac{Q^2T}{9A^3}$$

Variation of energy with respect to depth; Discharge "form", incorporating topwidth.

$$Fr^{2} = \frac{Q^{2}T}{gA^{3}}$$

At critical depth the gradient is equal to zero, therefore:

- Right hand term is a squared Froude number. Critical flow occurs when Froude number is unity.
- •Froude number is the ratio of inertial (momentum) to gravitational forces

DEPTH-AREA

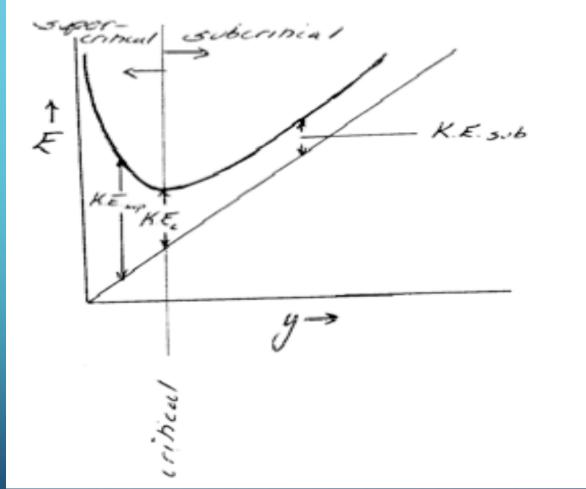
• The topwidth and area are depth dependent and geometry dependent functions:

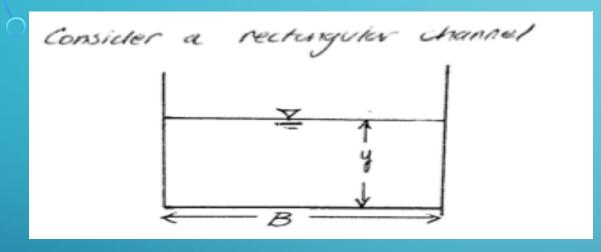
$$T = T(y)$$
 (topwidth is a function of depth)

 $A = A(y)$ (Flow over is a function of depth)

SUPER/SUB CRITICAL FLOW

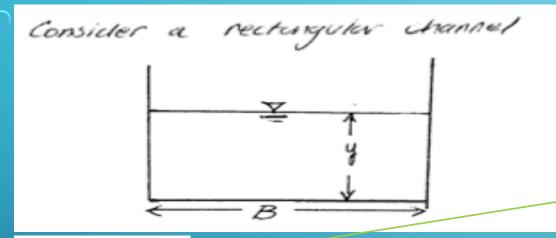
- Supercritical flow when KE >
 KE_{c.}
- Subcritical flow when
 KE<KE_{c.}
 - Flow regime affects slope of energy gradient, which determines how one integrates to find HGL.





Depth-Area Function:

Depth-Topwidth Function:

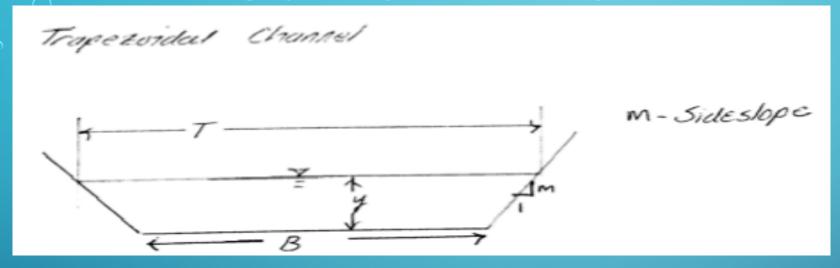


Substitute functions

$$J = \frac{Q^2 T}{g A^3} = \frac{Q^2 B}{g B^3 y^3} = \frac{Q^2}{g B^2 y^3}$$

Solve for critical depth

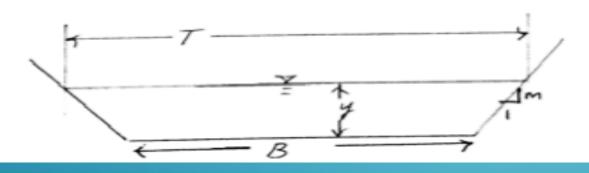
Compare to Eq. 3.104, pg 123)



Depth-Area Function:

Depth-Topwidth Function:





m-Sideslope

Substitute functions

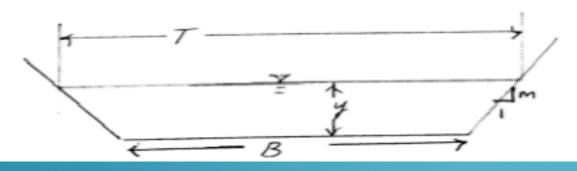
$$J = \frac{Q^{2}T}{gA^{3}} = \frac{Q^{2}(B + \frac{2y}{m})}{g(By + y^{2}/m)^{3}}$$

T(y) = B + 24

Solve for critical depth,
By trial-and-error is adequate.

Can use HEC-22 design charts.

Trapezoidal Channel



al-and-error:

$$I = \frac{(500)^2}{32.2} \cdot \frac{(20 + 29)}{(209 + 9^2)^3} = Fr^2(y)$$

Q = 500ft3/s

$$B = 20 ft$$

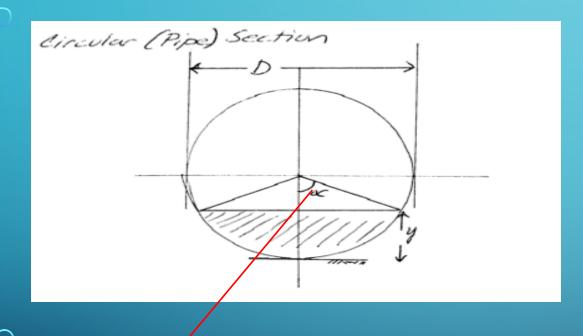
 $m = 1$

20 ft Guess this values

Adjust from Fr

y	Fr (y)	Remarks
-	18.4	- to big (superconticut)
2	2.2	- too big
3	0.6	+ to small (subcriticus)
2.5	1.09	+ very close
2.56	1.01	← acceptable (critical)

$I = \frac{Q^{2}T}{gA^{3}} = \frac{Q^{2}(B + \frac{2y}{m})}{g(By + y^{2}/m)^{3}}$



The most common sewer geometry (see pp 236-238 for similar development)

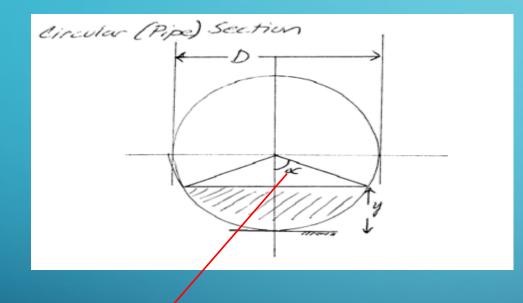
Depth-Topwidth:

Depth-Area:

Remarks:

Some references use radius and not diameter. If using radius, the half-angle formulas change. DON'T mix formulations.

These formulas are easy to derive, be able to do so!



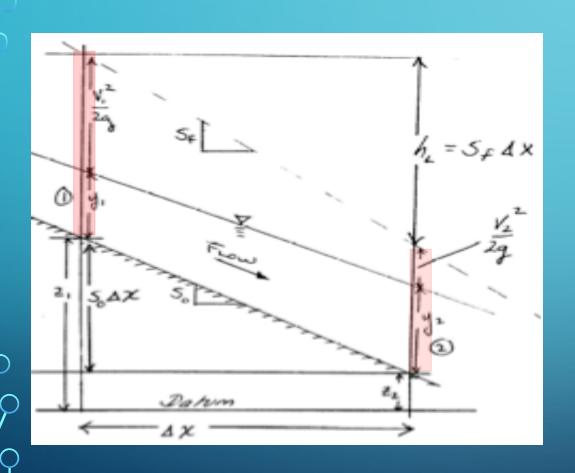
The most common sewer geometry (see pp 236-238 for similar development)

Depth-Topwidth:

Depth-Area:

Depth-Froude Number:

$$Fr^2(y) = \frac{Q^2 D sin x}{g(\frac{D^2}{4}(x-sin x \cos x))^3}$$



 Energy equation has two components, a specific energy and the elevation energy.

Energy Equation from
$$0 \rightarrow 0$$

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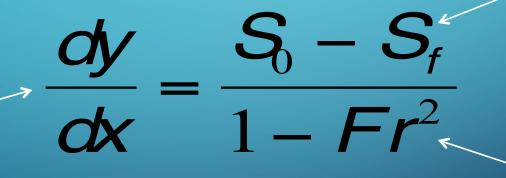
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Sketch of gradually varied flow.

Equation relating slope of water surface, channel slope, and energy slope:



Discharge and Section Geometry

Discharge and Section Geometry

Variation of Water Surface Elevation

Procedure to find water surface profile is to integrate the depth taper with distance:

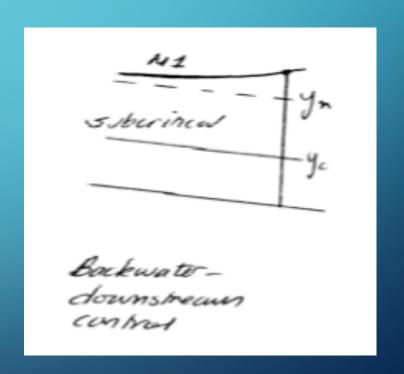
$$HGL(x) = \int_{x_0}^{x_1} \left(\frac{dy}{dx}\right) + \left(\frac{dz}{dx}\right) dx = \int_{x_0}^{x_1} \frac{S_0 - S_f}{1 - Fr^2} + \left(\frac{dz}{dx}\right) dx$$

CHANNEL SLOPES AND PROFILES

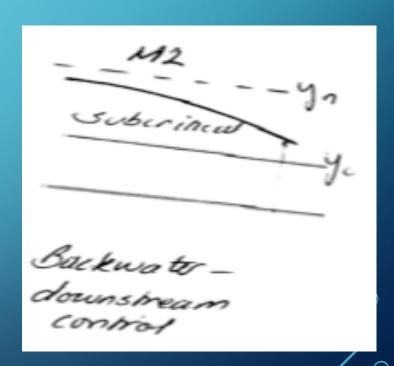
SLOPE	DEPTH RELATIONSHIP
Steep	$y_n < y_c$
Critical	$y_n = y_c$
Mild	$y_n > y_c$
Horizontal	$S_0 = 0$
Adverse	S ₀ < 0

PROFILE TYPE	DEPTH RELATIONSHIP
Type-1	$y > y_c$ AND $y > y_n$
Type -2	$y_c < y < y_n OR y_n < y < y_n$
Type -3	y < y _c AND y < y _n

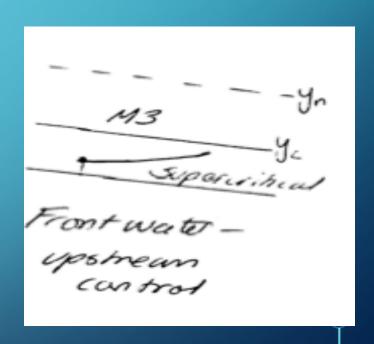
- All flows approach normal depth
 - M1 profile.
 - Downstream control
 - Backwater curve
 - Flow approaching a "pool"
 - Integrate upstream



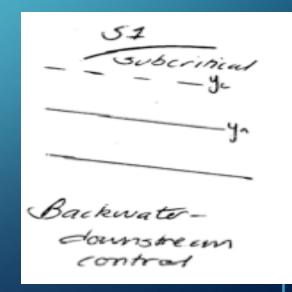
- All flows approach normal depth
 - M2 profile.
 - Downstream control
 - Backwater curve
 - Flow accelerating over a change in slope
 - Integrate upstream



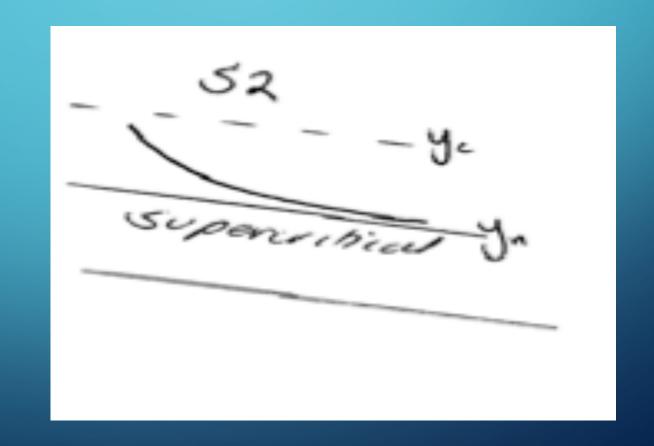
- All flows approach normal depth
 - M3 profile.
 - Upstream control
 - Backwater curve
 - Decelerating from under a sluice gate.
 - Integrate downstream



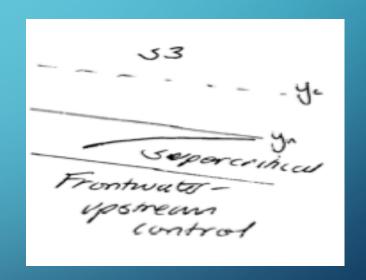
- All flows approach normal depth
 - S1 profile.
 - Downstream control
 - Backwater curve
 - Integrate upstream



- All flows approach normal depth
 - S2 profile.



- All flows approach normal depth
 - S3 profile.
 - Upstream control
 - Frontwater curve
 - Integrate downstream



- Numerous other examples, see any hydraulics text (Henderson is good choice).
- Flow profiles identify control points to start integration as well as direction to integrate.

WSP USING ENERGY EQUATION

- Variable Step Method
 - Choose y values, solve for space step between depths.
 - Non-uniform space steps.
 - Prisimatic channels only.

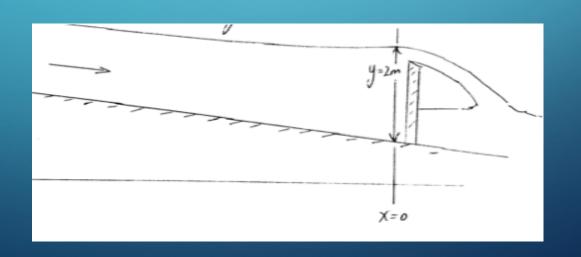
$$E_{f} + S_{0} \Delta \chi = E_{2} + S_{f} \Delta \chi \qquad Solve Ev \Delta \chi$$

$$\Delta \chi = \frac{E_{2} - E_{f}}{S_{0} - S_{f}}$$

WSP ALGORITHM

- O Start from a section with known depth.
- @ Calculate E, for starting section.
- (3) Calculate St, for storning section
- 4) Pertirb depth slightly, calculate new Ez
- 3 Calculate Sp at new section
- 6) Compute average tricken slope Sp
- (7) Solve for AX.
- (8) Move to rext section and repeat

Rectangular Channel, B = 1m, $Q = 2.5m^3/s$ $S_0 = 0.001$, N = 0.025. Water Hows over a weir at y = 2.0m just Upstream of weir. Compute W.s.P.



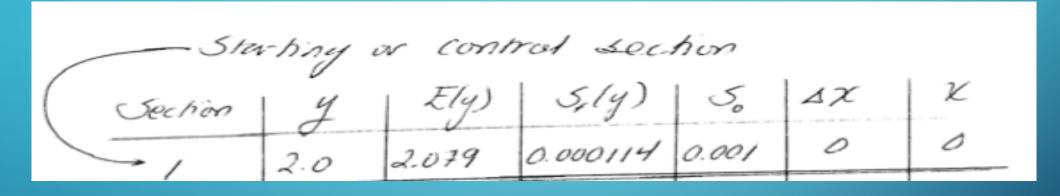
Energy/depth function

$$E = \frac{Q^2}{2gA^2} + 4f = \frac{(2.5)^2}{2(9.8)(m)(y)^2} + 4f = \frac{0.32}{4^2} + 4f$$

Friction slope function

$$S_{F} = \frac{n^{2}Q^{2}}{A^{2}R_{n}^{4/3}} = \frac{n^{2}(2.5)^{2}}{y^{2}(\frac{4}{1+2y})^{4/3}}$$

Start at known section



Compute space step (upstream)

Enter in
$$\Delta \chi_{132} = \frac{1.898 - 2.079}{0.001 - 0.000135} = \frac{-0.181}{0.000865} = -209.3$$

Start at known section

51a	hny	or cont	rol sec	hon		
Section	4	Ely)	5,14)	5	AX	K
			0.000114		0	0
2			0.000157		-209.3	-209.3

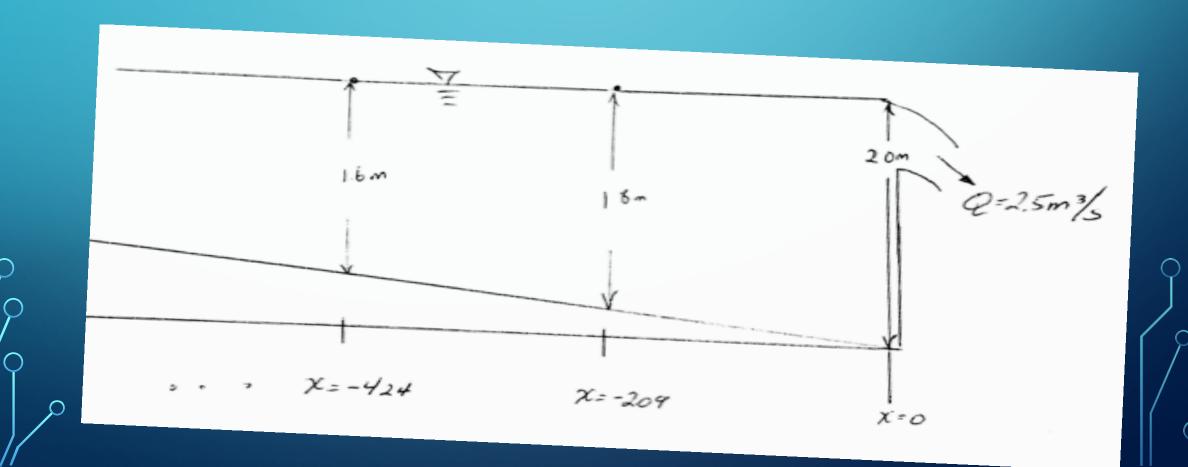
• Compute space step (upstream)

$$\Delta Y_{2 \to 3} = \frac{1.724 - 1.898}{0.001 - 0.000191} = \frac{-0.174}{0.000809} = -215.1$$

Continue to build the table

Starting or control section											
Section	1 4	Ely)	5,14)	5	AX	K					
	· //	2.079	0.000114	0.001	0	0					
2	i		0.000157			-209.3					
3	1.6	1.724	0.000225	0.001	-215.1	-4/24.3					

Use tabular values and known bottom elevation to construct WSP.



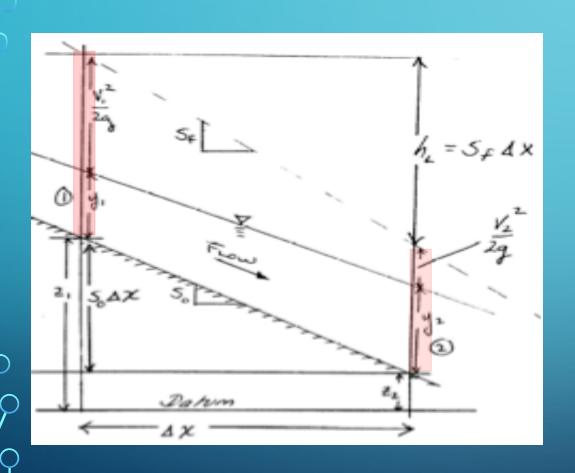
WSP FIXED STEP METHOD

Fixed step method rearranges the energy equation differently:

$$E_2 = E_1 + \frac{S_0 - S_f}{A}$$

- $E_2=E_1+\frac{S_0-S_f}{\Delta x}$ Right hand side and left hand side have the unknown "y" at section 2.
 - Implicit, non-linear difference equation.
 - Use SWMM or HEC-RAS for this (or take Open Channel Flow class)

GRADUALLY VARIED FLOW



Apply WSP computation to a circular conduit

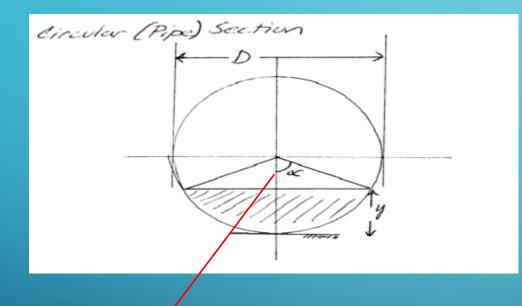
Energy Equation from
$$0 \rightarrow 0$$

$$\frac{\sqrt{2}}{2y} + y, +2, = \frac{\sqrt{2}}{2g} + y_2 + 2z + h_2$$

$$E, \qquad E_2 \qquad - Specific energy at each section$$

Sketch of gradually varied flow.

DEPTH-AREA RELATIONSHIP



The most common sewer geometry (see pp 236-238 for similar development)

Depth-Topwidth:

Depth-Area:

Depth-Froude Number:

$$Fr^{2}(y) = \frac{Q^{2} D sin \kappa}{g\left(\frac{D^{2}}{4}(\alpha - sin \kappa \cos \kappa)\right)^{3}}$$

- Compute WSE in circular pipeline on 0.001 slope.
- Manning's n=0.02
- Q = 11 cms
- D = 10 meters
- Downstream control depth is 8 meters.

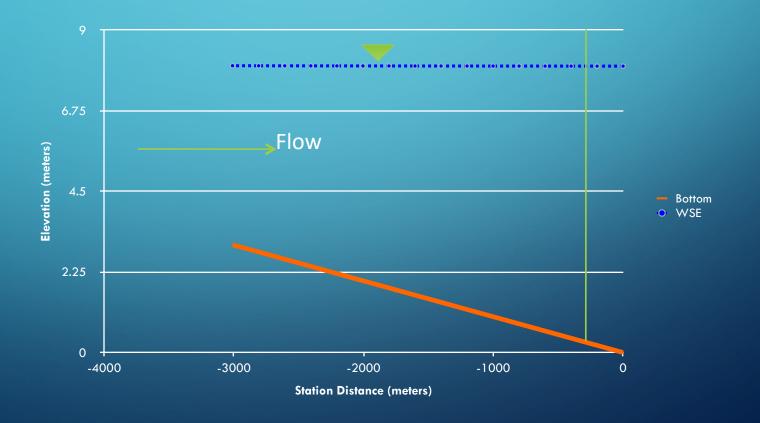
Use spreadsheet, start at downstream control.

GVF Worksheet Variable Step Method														
Q(cm	s) 11													
n	0.02													
Section	n Depth	Diame	Alpha	Area	Pw	Rh	Velocity	Energy	Friction S	Bottom	Delta x	Bottom	WSE	Station
Section	n Depth L 8			1				Energy 8.001		Bottom 0.001				Station 0
Section		10	2.2143	67.4	22.14	3.04	0.163		2E-06		0	0		Station 0 -200

Compute Delta X, and move upstream to obtain station positions.

GVF Wo	rkshee	t Va	riable Ste	p Metho	d									
Q(cms)	11													
n	0.02													
Section	Depth	Diame	Alpha	Area	Pw	Rh	Velocity	Energy	Friction S	Bottom	Delta x	Bottom	WSE	Station
1	8	10	2.2143	67.4	22.14	3.04	0.163	8.001	2E-06	0.001	0	0	8	0
2	7.8	10	2.1652	65.7	21.65	3.04	0.167	7.801	3E-06	0.001	-200	0.2	8	-200
3	7.6	10	2.1176	64	21.18	3.02	0.172	7.602	3E-06	0.001	-200	0.401	8.001	-401
4	7.4	10	2.0715	62.3	20.71	3.01	0.177	7.402	3E-06	0.001	-200	0.601	8.001	-601
5	7.2	10	2.0264	60.5	20.26	2.99	0.182	7.202	3E-06	0.001	-201	0.802	8.002	-802
6	7	10	1.9823	58.7	19.82	2.96	0.187	7.002	3E-06	0.001	-201	1.002	8.002	-1002
7	6.8	10	1.9391	56.9	19.39	2.93	0.193	6.802	4E-06	0.001	-201	1.203	8.003	-1203
8	6.6	10	1.8965	55	18.97	2.9	0.2	6.602	4E-06	0.001	-201	1.404	8.004	-1404
9	6.4	10	1.8546	53.1	18.55	2.86	0.207	6.402	4E-06	0.001	-201	1.604	8.004	-1604
10	6.2	10	1.8132	51.2	18.13	2.82	0.215	6.202	5E-06	0.001	-201	1.805	8.005	-1805
11	6	10	1.7722	49.2	17.72	2.78	0.224	6.003	5E-06	0.001	-201	2.006	8.006	-2006
12	5.8	10	1.7315	47.2	17.31	2.73	0.233	5.803	6E-06	0.001	-201	2.207	8.007	-2207
13	5.6	10	1.6911	45.3	16.91	2.68	0.243	5.603	7E-06	0.001	-201	2.408	8.008	-2408
14	5.4	10	1.6509	43.3	16.51	2.62	0.254	5.403	8E-06	0.001	-201	2.609	8.009	-2609
15	5.2	10	1.6108	41.3	16.11	2.56	0.267	5.204	9E-06	0.001	-201	2.81	8.01	-2810
16	5	10	1.5708	39.3	15.71	2.5	0.28	5.004	9E-06	0.001	-201	3.011	8.011	-3011

Use Station location, Bottom elevation and WSE to plot water surface profile.



NEXT TIME

Introduction to SWMM