

TXHYETO.XLS:

A Tool To Facilitate Use of Texas-Specific Hyetographs for Design Storm Modeling

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Acknowledgements

- Funding and direction provided by the Texas Department of Transportation through research contract 0-6824, “New Rainfall Coefficients”

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Outline

- Overview
- Methods Currently in Use
 - Empirical, Dimensionless Hyetographs (Williams-Sether, 2004)
 - Graphical Method
 - Linear Interpolation
- Proposed Alternative Method
 - Distribution Mixture Model

Overview

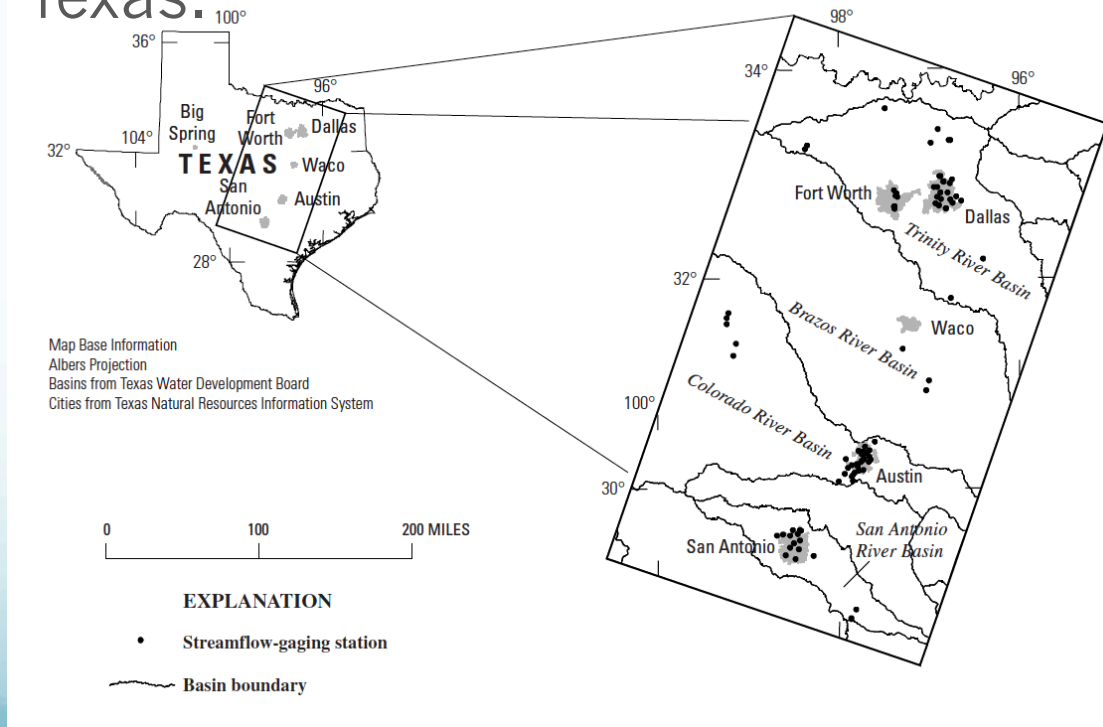
- Empirical, Dimensionless, Cumulative Rainfall Hyetographs Developed for Selected Watersheds in Texas
- The graphical method for dimensional modeling found using the Texas Dimensionless Hyetographs is widely used but is limited with small or non-incremental time steps
- Two methods of interpolation were explored
 - Linear interpolation
 - Distribution-mixture function
- TXHYETO.XLS, a provisional tool, was created

Texas Dimensionless Hyetographs

- Texas-specific storm hyetographs were reported in Williams-Sether et. al. (2004) as a design storm tool for use in drainage design
- These hyetographs are limited because of difficulty in “dimensionalizing” the tabulated hyetograph values for use in hydrologic software (SWMM/HECHMS)
- Difficulties in dimensionalizing is two-fold
 - Tabulated values must be rescaled into dimensional values
 - Dimensionalized tabulation time intervals may not correspond to the time intervals of interest

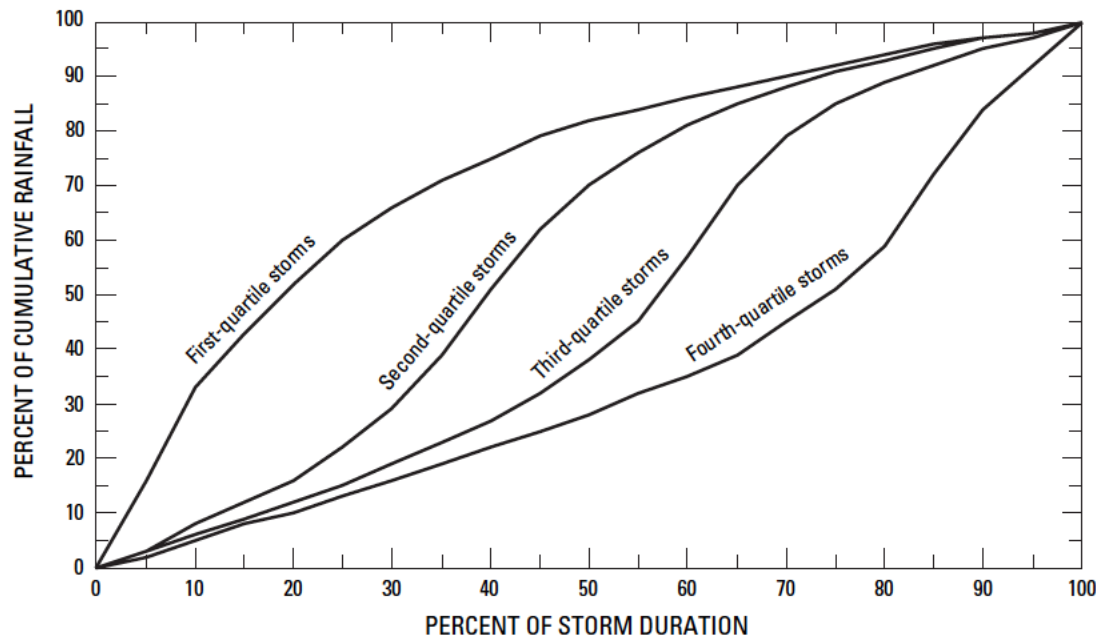
Texas Dimensionless Hyetographs

- Williams-Sether et. al. (2004) analyzed data from over 1,600 runoff-producing storms at 91 USGS streamflow-gauging stations in North and South Central Texas.

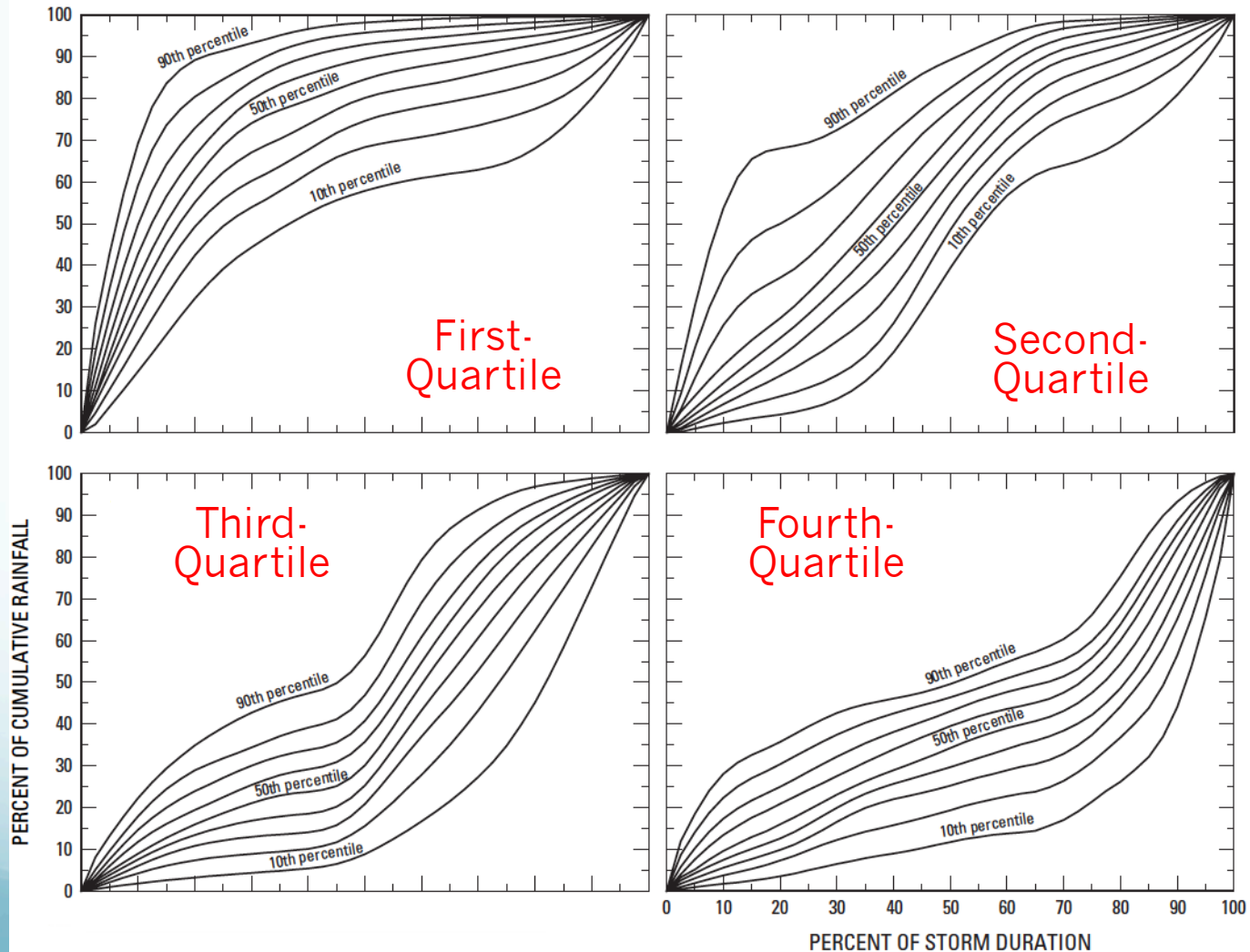


Texas Dimensionless Hyetographs

- They developed empirical, dimensionless, cumulative-rainfall hyetographs.
- Storm-quartile classifications were determined using Huff 1967, and 1990 type classification



Texas Dimensionless Hyetographs



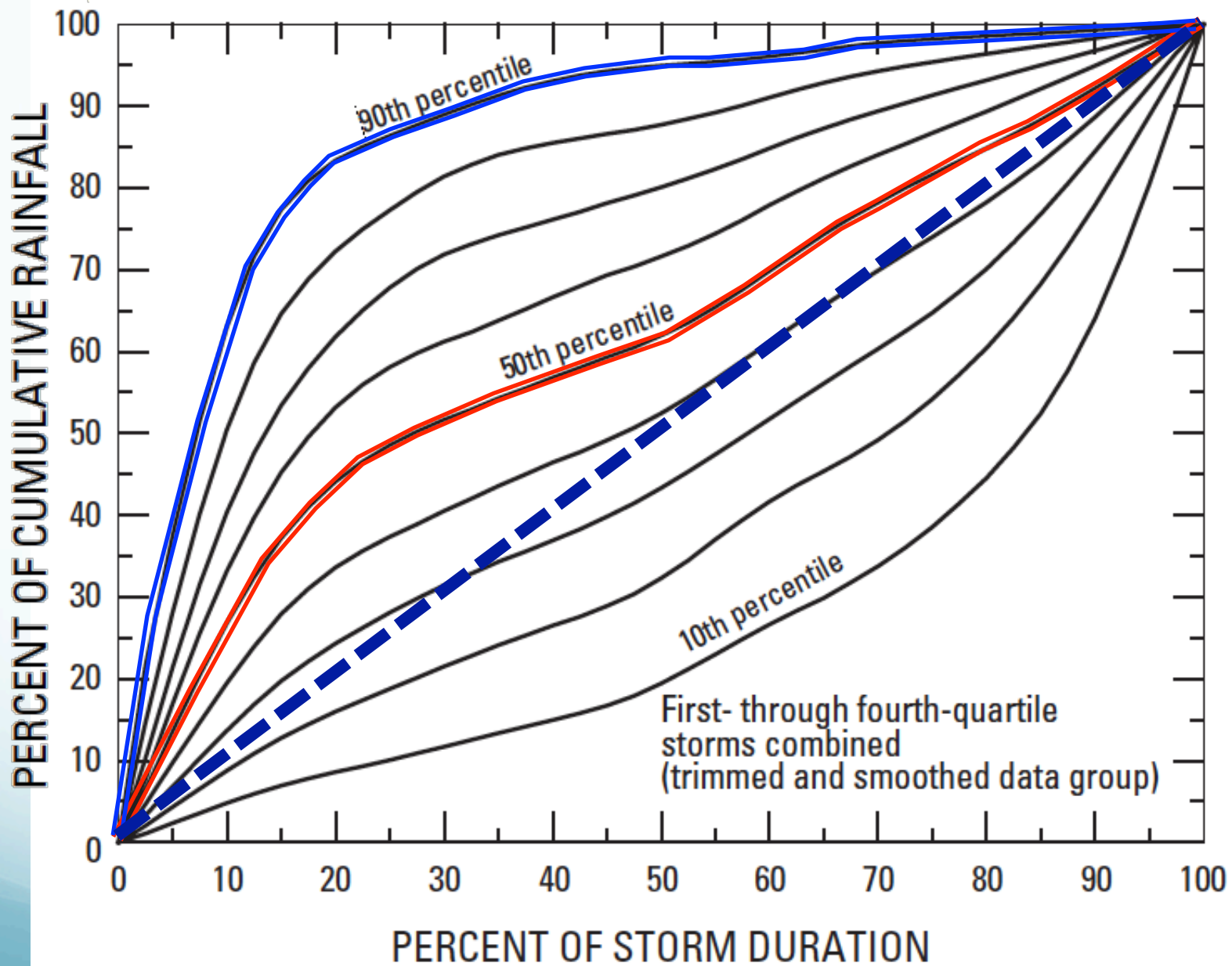
Texas Dimensionless Hyetographs

- A combined dimensionless family of envelopes was produced
- Presented in both graphical and tabular form.
- Used to estimate distributions of rainfall with time for Texas watersheds drainage areas of <160 mi².

Supplement 5. Trimmed and smoothed percentiles for empirical hyetograph analysis, 1959–86.—Continued

[The interval is the center of the percent-of-storm-duration interval; —, no data]

Interval	Percentile										
	10th	20th	25th	30th	40th	50th	60th	70th	75th	80th	90th
First- through fourth-quartile storms combined; storm duration 0 to 72 hours											
2.5	1.08	2.04	2.58	3.34	4.69	6.37	7.81	10.30	12.16	14.66	21.60
5.0	2.35	4.32	5.47	6.84	9.74	13.58	16.97	21.38	24.48	28.12	37.57
7.5	3.59	6.56	8.32	10.27	14.68	20.49	25.56	31.57	35.63	40.20	51.55
10.0	4.82	8.78	11.16	13.68	19.47	26.83	33.19	40.38	45.16	50.47	63.04
12.5	5.92	10.85	13.80	16.85	23.94	32.42	39.68	47.57	52.72	58.62	71.66
15.0	6.92	12.77	16.23	19.72	27.91	37.21	45.23	53.41	58.54	64.61	77.38
17.5	7.80	14.43	18.29	22.14	31.01	41.00	49.56	57.96	62.97	68.83	80.89
20.0	8.60	15.99	20.23	24.32	33.59	44.11	53.16	61.80	66.74	72.25	83.32
22.5	9.31	17.38	21.89	26.21	35.63	46.55	55.92	65.02	69.84	74.94	85.01
25.0	10.06	18.75	23.51	28.07	37.35	48.54	58.09	67.80	72.62	77.28	86.35
27.5	10.87	20.11	25.00	29.79	38.88	50.23	59.80	70.07	75.06	79.47	87.66
30.0	11.70	21.51	26.51	31.41	40.52	51.68	61.22	71.87	76.92	81.38	88.96
32.5	12.51	22.77	27.81	32.85	42.01	52.90	62.34	73.12	78.10	82.81	90.18
35.0	13.35	24.09	29.22	34.30	43.56	54.27	63.76	74.21	79.02	84.02	91.29
37.5	14.16	25.27	30.47	35.54	44.99	55.49	65.16	75.15	79.64	84.83	92.25
40.0	14.96	26.51	31.85	36.89	46.42	56.80	66.62	76.11	80.22	85.47	93.05
42.5	15.78	27.58	33.21	38.24	47.68	58.03	67.98	77.06	80.86	86.03	93.72
45.0	16.71	28.90	34.80	39.80	49.13	59.31	69.33	78.12	81.72	86.61	94.24
47.5	17.89	30.35	36.44	41.44	50.66	60.49	70.35	79.07	82.56	87.09	94.64
50.0	19.41	32.28	38.33	43.33	52.45	61.97	71.60	80.06	83.51	87.72	94.92
52.5	21.16	34.45	40.32	45.28	54.39	63.51	72.89	81.15	84.53	88.42	95.18
55.0	22.94	36.99	42.49	47.39	56.57	65.39	74.37	82.30	85.61	89.20	95.40
57.5	24.82	39.38	44.67	49.56	58.80	67.56	76.05	83.52	86.75	90.06	95.70
60.0	26.62	41.64	46.83	51.75	61.09	69.85	77.89	84.82	88.01	91.04	96.06
62.5	28.29	43.62	49.00	53.94	63.38	72.11	79.55	86.10	89.22	91.97	96.47
65.0	29.86	45.38	50.95	56.07	65.59	74.32	81.14	87.25	90.31	92.83	96.90
67.5	31.76	47.16	52.88	58.23	67.77	76.38	82.65	88.36	91.31	93.60	97.32
70.0	33.75	49.16	54.81	60.32	69.87	78.21	84.02	89.37	92.17	94.27	97.68
72.5	36.00	51.52	56.94	62.47	71.97	80.00	85.35	90.35	92.90	94.84	97.97
75.0	38.51	54.15	59.24	64.72	73.98	81.61	86.69	91.30	93.55	95.38	98.19
77.5	41.45	57.17	62.09	67.30	76.10	83.25	88.02	92.25	94.20	95.89	98.38
80.0	44.54	60.42	65.22	70.08	78.24	84.84	89.34	93.15	94.86	96.39	98.56
82.5	48.24	64.13	68.85	73.31	80.60	86.54	90.72	94.08	95.54	96.87	98.72
85.0	52.41	68.26	72.78	76.77	83.07	88.30	92.09	94.98	96.22	97.34	98.90
87.5	57.68	72.90	77.10	80.53	85.81	90.21	93.49	95.87	96.93	97.81	99.09
90.0	64.02	77.90	81.55	84.43	88.65	92.18	94.92	96.75	97.61	98.28	99.29
92.5	71.71	83.28	86.22	88.48	91.66	94.22	96.37	97.65	98.29	98.75	99.49
95.0	80.43	88.80	90.85	92.47	94.62	96.21	97.81	98.54	98.96	99.22	99.70
97.5	90.01	94.42	95.53	96.53	97.64	98.21	99.26	99.44	99.65	99.70	99.92



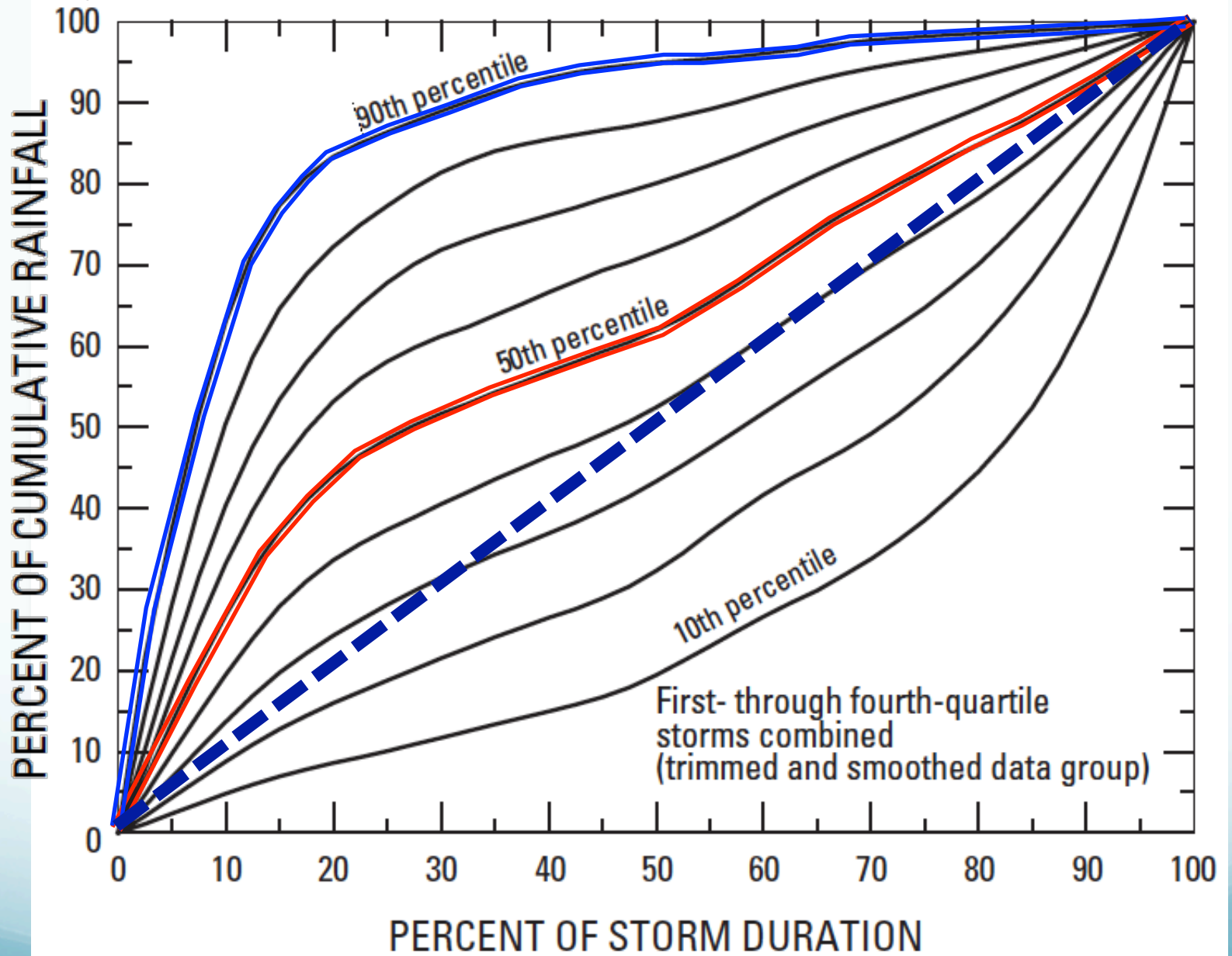
Dimensionalization

- Requires the user to rescale the time and percent cumulative rainfall into actual durations and total storm depth.
- Engineer must determine the depth for a particular duration
 - Various of tools to do this in Texas:
 - Asquith and Roussel (2004) and Asquith (1998) (DDF Atlas)
 - Frederick et. Al (1997)
 - Hershfield (1961) (TP-40)
 - EBDLKUP-NEW (a companion product for this project)
 - Examples of tools elsewhere:
 - NOAA Atlas 14

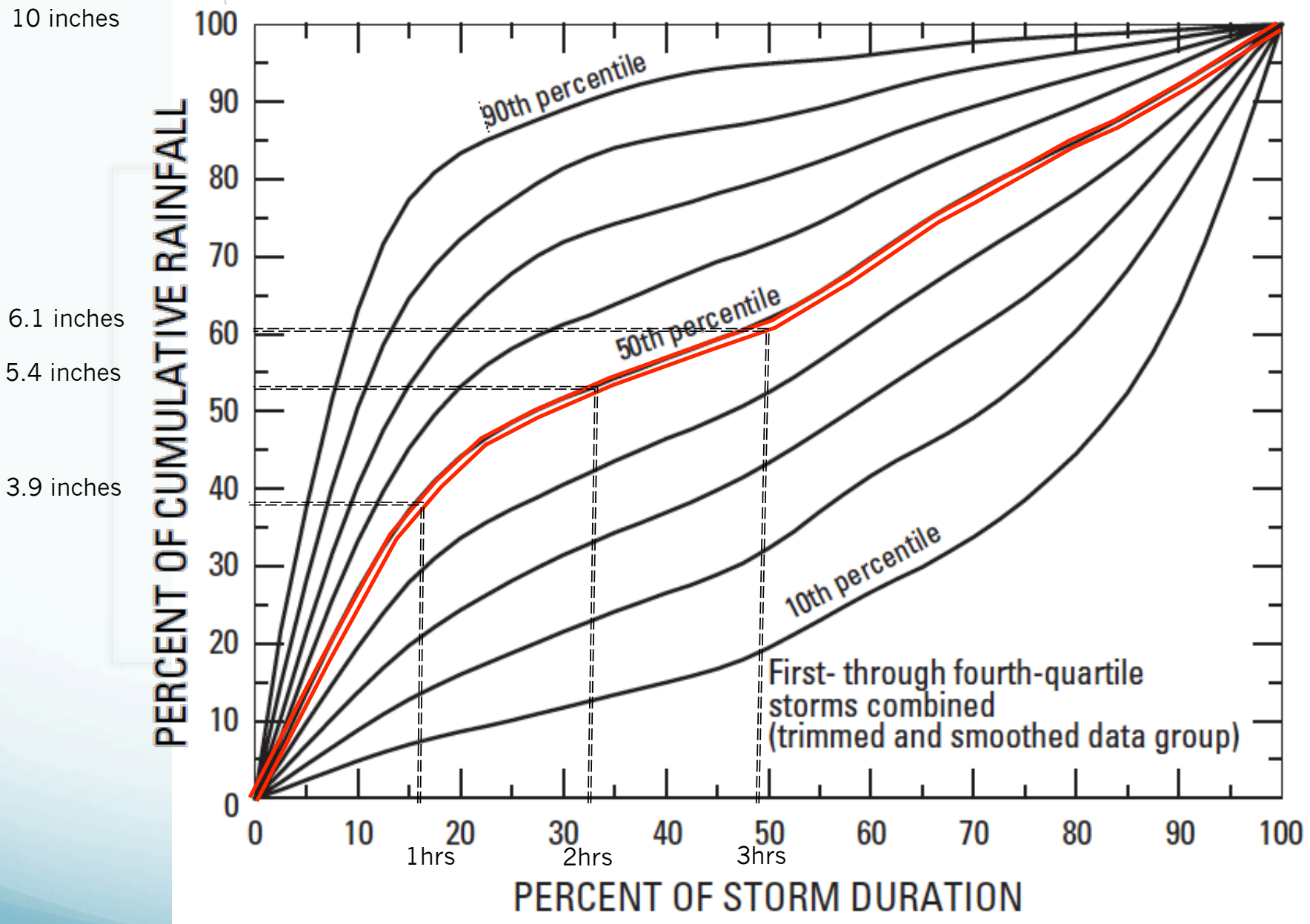
Example of Rescaling Axes

- Example
 - Suppose a 4% chance (25 year) , 6 hour storm in Texas has an anticipated depth of 10 inches
 - After rescaling, the horizontal axis would range from 0 to 6 hours
 - After rescaling, the vertical axis would range from 0 to 10 inches

Rescale Depth



Rescale Time



Alternative Method-Linear Interpolation

- An initial alternative method of Linear Interpolation was explored using Excel
- Linear Interpolation takes specified values of depth and duration, rescales them, and exports time and depth for time steps specified by user

Methodology

- User chooses desired time step
- Reprogramming is necessary for different time steps

	A	B	C	D	E	F	G	H	I	J	K
1	Interpolated Hyetograph			Interpolation Points based on Time in A3 to A+Max				Dimensional Hyetograph (from Tables)			
2	Time(min)	Time(hrs)	Depth(in)	T-low	T-high	D-low	D-high	Time(Hrs)	Depth (in)		
3	0	0.00	0.00	0	0.15	0	0.637	0	0	0	
4	15	0.25	1.12	0.15	0.3	0.637	1.358	0.150	0.637		
5	30	0.50	2.26	0.45	0.6	2.049	2.683	0.300	1.358		
6	45	0.75	3.24	0.75	0.9	3.242	3.721	0.450	2.049		
7	60	1.00	3.97	0.9	1.05	3.721	4.1	0.600	2.683		
8	75	1.25	4.49	1.2	1.35	4.411	4.655	0.750	3.242		
9	90	1.50	4.85	1.5	1.65	4.854	5.023	0.900	3.721		
10	105	1.75	5.12	1.65	1.8	5.023	5.168	1.050	4.1		
11	120	2.00	5.34	1.95	2.1	5.29	5.427	1.200	4.411		
12	135	2.25	5.55	2.25	2.4	5.549	5.68	1.350	4.655		
13	150	2.50	5.76	2.4	2.55	5.68	5.803	1.500	4.854		
14	165	2.75	5.97	2.7	2.85	5.931	6.049	1.650	5.023		
15	180	3.00	6.20	3	3.15	6.197	6.351	1.800	5.168		
16	195	3.25	6.48	3.15	3.3	6.351	6.539	1.950	5.29		
17	210	3.50	6.83	3.45	3.6	6.756	6.985	2.100	5.427		
18	225	3.75	7.21	3.75	3.9	7.211	7.432	2.250	5.549		
19	240	4.00	7.57	3.9	4.05	7.432	7.638	2.400	5.68		
20	255	4.25	7.88	4.2	4.35	7.821	8	2.550	5.803		
21	270	4.50	8.16	4.5	4.65	8.161	8.325	2.700	5.931		
22	285	4.75	8.43	4.65	4.8	8.325	8.484	2.850	6.049		
23	300	5.00	8.71	4.95	5.1	8.654	8.83	3.000	6.197		
24	315	5.25	9.02	5.25	5.4	9.021	9.218	3.150	6.351		
25	330	5.50	9.35	5.4	5.55	9.218	9.422	3.300	6.539		
26	345	5.75	9.69	5.7	5.85	9.621	9.821	3.450	6.756		
27	360	6.00	10.00	6	1E+09	10	10	3.600	6.985		
28								3.750	7.211		
29								3.900	7.432		
30								4.050	7.638		
31								4.200	7.821		
32								4.350	8		
33								4.500	8.161		
34								4.650	8.325		
35								4.800	8.484		
36								4.950	8.654		
37								5.100	8.83		
38								5.250	9.021		
39								5.400	9.218		
40								5.550	9.422		
41								5.700	9.621		
42								5.850	9.821		
43								6	10		
44								1000000006	10		
45											

=G3+(H3-G3)*(B3-E3)/(F3-E3)

=INDEX(\$I\$3:\$I\$43,MATCH(B3,\$I\$3:\$I\$43,1))

=INDEX(\$I\$3:\$I\$43,MATCH(B3,\$I\$3:\$I\$43,1)+1)

=INDEX(\$J\$3:\$J\$43,MATCH(B3,\$I\$3:\$I\$43,1))

=INDEX(\$J\$3:\$J\$43,MATCH(B3,\$I\$3:\$I\$43,1)+1)

This row fixed set Time = DURATION + 1.0E-9 or the search will fail last row of interpolation

Alternative Method-Distribution Mixture Model

- Linear interpolation method is situation specific
- Distribution-mixture model
 - fits smooth functions to the tabulation values from Texas Dimensionless Hyetograph
 - can be used to directly estimate time-depth pairs
 - Time depth pairs can be directly input into computer based runoff modeling software (SWMM/HECHMS)

Distribution-Mixture Model

- Several candidate functions were explored based on the shape of the 50th and 90th percentile curves
- A function built from a mixture of two distributions was selected as the best fit functional form because it was able to reproduce the shape of the dimensionless hyetographs over the entire range of the dimensionless storm better than the other functions researched .
- The functional form was fit using a non-linear least-squares approach where the difference between the model value and the tabulated value were minimized by changing the values of the parameters

Methodology

- Distribution-mixture function model

$$D^*(t^*) = w_1(I_{t^*}(\alpha, \beta)) - w_2\left(\frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(t^*-\mu)^2}{2\sigma^2}\right)\right)$$

where

$D^*()$ is the dimensionless depth of precipitation as a function of dimensionless time.

t^* is the dimensionless time.

w_1 is a weighting parameter.

α is a shape parameter for the Beta distribution.

β is a shape parameter for the Beta distribution.

w_2 is a weighting parameter.

μ is the mean (used to locate the mode of the function in this work).

σ is the standard deviation (used to control the width of the function in this work).

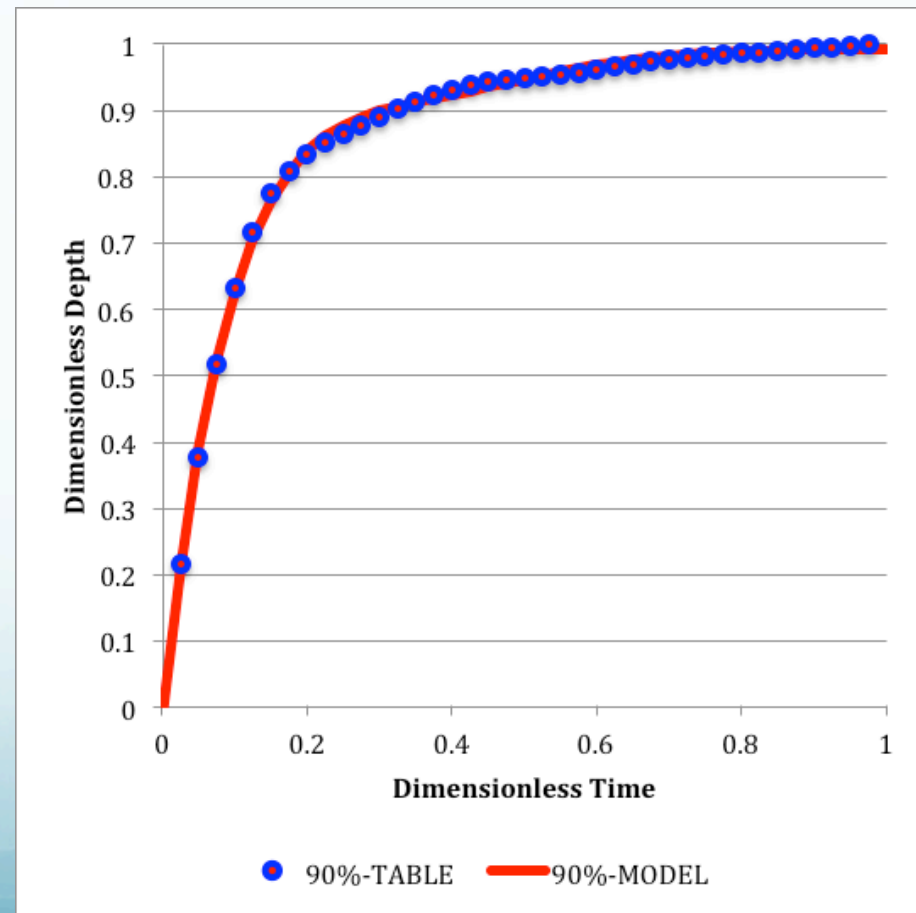
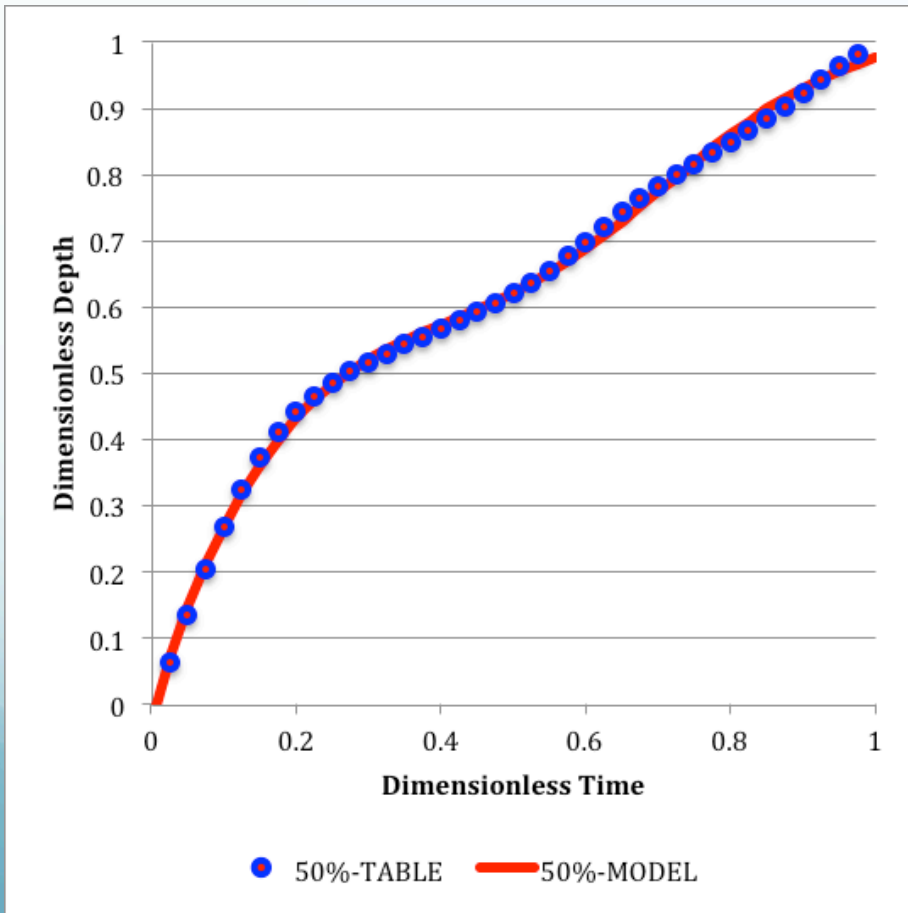
Parameter Estimation

- The functional form was fit using a non-linear least-squares approach.
- The difference between the model value and the tabulated values were minimized by changing the parameters.
- Excel Solver (GRG Algorithm) was used.
 - Program defaults were used with initial estimates by trial-and-error

$$D^*(t^*) = w_1(I_{t^*}(\alpha, \beta)) - w_2\left(\frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(t^*-\mu)^2}{2\sigma^2}\right)\right)$$

Distribution-Mixture Model

- Comparison of Williams-Sether tabulated values to distribution-mixture model function



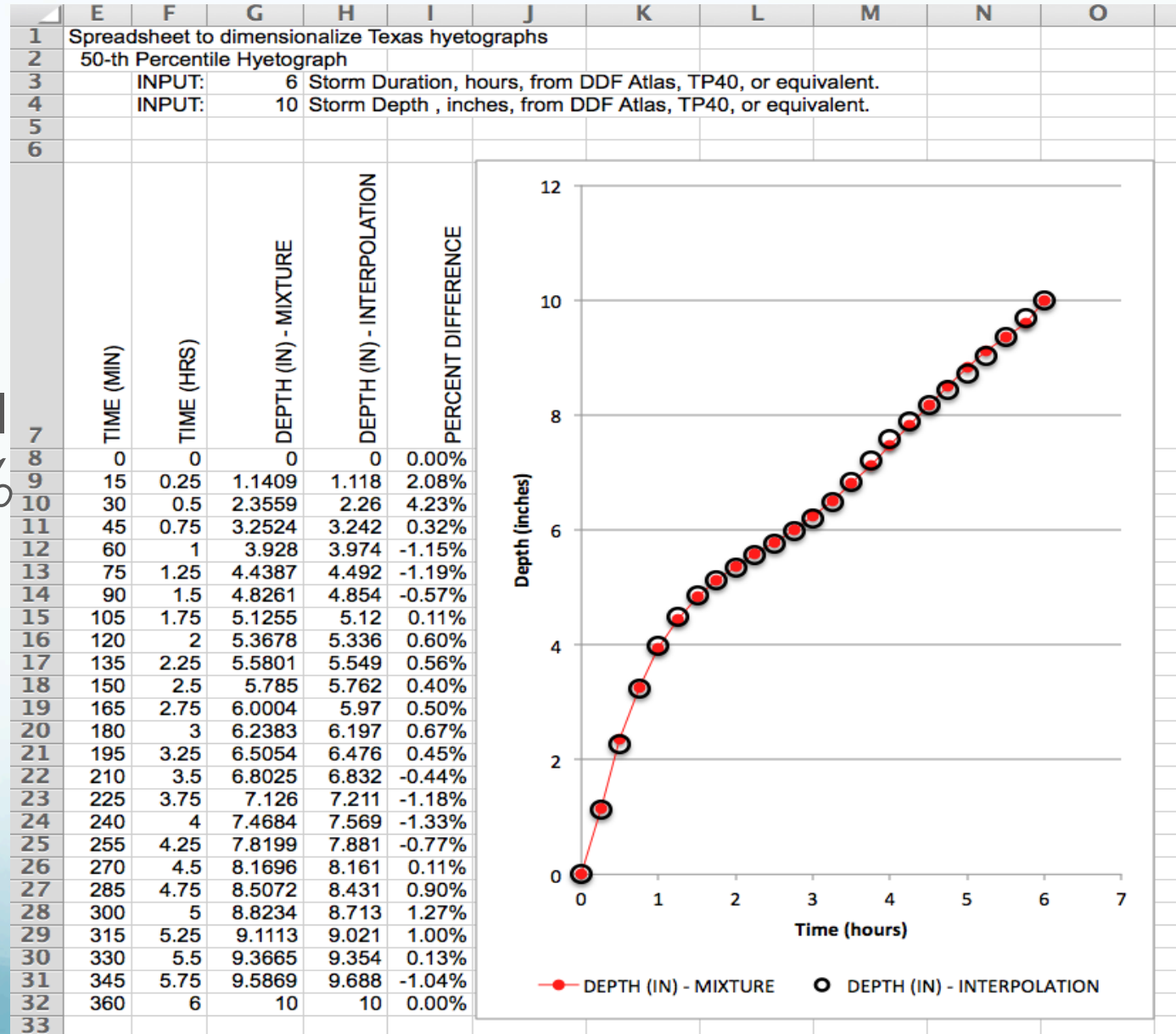
TXHYETO.XLS

	A	B	C	D	E	F	G	H	I	J	K	L
1	Spreadsheet to dimensionalize Texas hyetographs										Mixture Model Parameters	
2	50th Percentile Hyetograph										w ₁	1.038977414
3		INPUT:	6	Storm Duration, hours, from DDF Atlas, TP40, or equivalent.							α	0.795462882
4		INPUT:	10	Storm Depth, inches, from DDF Atlas, TP40, or equivalent.							β	3.485892325
5										w ₂	0.248832841	
6										μ	0.471873548	
7	TIME (MIN)	TIME (HRS)	DEPTH (IN)							σ	0.283390998	
8	0	0	0									
9	15	0.25	1.14086									
10	30	0.5	2.355945									
11	45	0.75	3.252356									
12	60	1	3.928036									
13	75	1.25	4.438726									
14	90	1.5	4.826142									
15	105	1.75	5.125504									
16	120	2	5.367787									
17	135	2.25	5.580054									
18	150	2.5	5.785012									
19	165	2.75	6.000375									
20	180	3	6.238334									
21	195	3.25	6.505373									
22	210	3.5	6.802513									
23	225	3.75	7.126003									
24	240	4	7.468401									
25	255	4.25	7.819879									
26	270	4.5	8.16963									
27	285	4.75	8.507161									
28	300	5	8.823376									
29	315	5.25	9.111306									
30	330	5.5	9.366478									
31	345	5.75	9.586911									
32	360	6	10									
33												
34												
35												

=IF(B8<=0,0,IF(B8>=\$C\$3,\$C\$4,(\$K\$2*(BETA.DIST(B8/\$C\$3,\$K\$3,\$K\$4,TRUE,0,1))-\$K\$5*NORM.DIST(B8/\$C\$3,\$K\$6,\$K\$7,FALSE))*\$C\$4))

Comparison

- Compare the interpolation and distribution-mixture model – less than 5% difference



HEC-HMS Example

HEC-HMS

- TXHYETO.XLS efficiently supplies design storms for Texas into HEC-HMS or SWMM
- Example for 6-hour storm with 15 min. increments

Input desired time increments (15 min. for this example) →

The screenshot shows the 'Time-Series Gage' dialog box in HEC-HMS. The 'Name' field is 'TXHYETO-DesignStorm'. The 'Data Source' is 'Manual Entry', 'Units' is 'Cumulative Inches', and 'Time Interval' is '15 Minutes'. The 'Latitude' and 'Longitude' fields are empty. The 'Time Interval' field is highlighted with a blue arrow pointing from the text on the left.

Field	Value
Name	TXHYETO-DesignStorm
Description	
Data Source	Manual Entry
Units	Cumulative Inches
Time Interval	15 Minutes
Latitude Degrees	
Latitude Minutes	
Latitude Seconds	
Longitude Degrees	
Longitude Minutes	
Longitude Seconds	

HEC-HMS

- The purpose of the tool is to simplify supplying design storms for Texas into HEC-HMS or SWMM.

Input desired storm duration (6-hour storm)

Name: TXHYETO-DesignStorm	
*Start Date (ddMMMYYYY)	01Jan2000
*Start Time (HH:mm)	00:00
*End Date (ddMMMYYYY)	01Jan2000
*End Time (HH:mm)	06:00

HEC-HMS

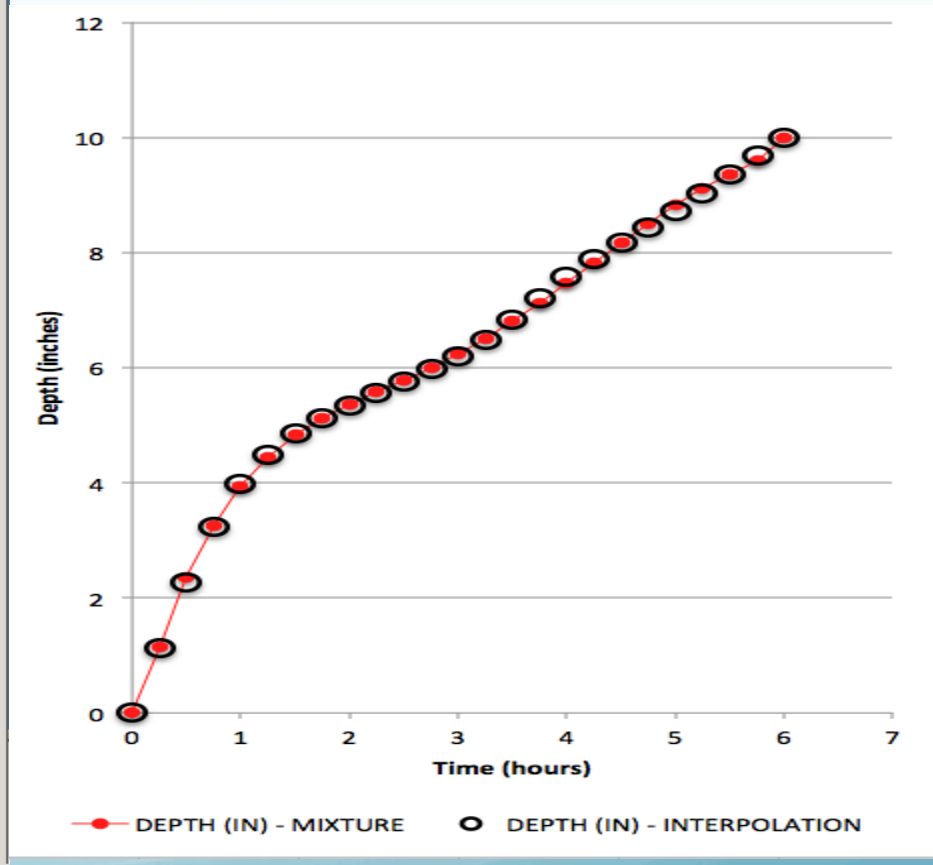
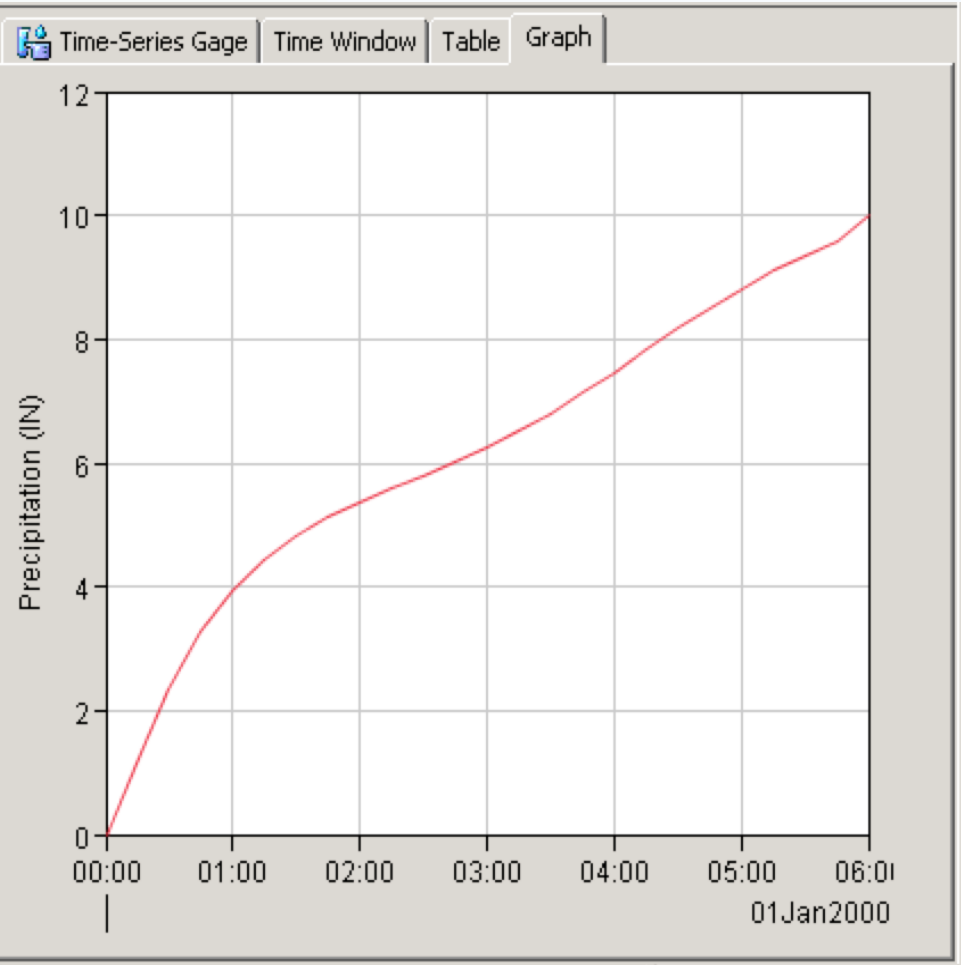
	A	B	C	D	E
1	Spreadsheet to dimensionalize Texas hyetographs				
2	50th Percentile Hyetograph				
3		INPUT:	6	Storm Duration, hou	
4		INPUT:	10	Storm Depth , inche	
5					
6					
7	TIME (MIN)	TIME (HRS)	DEPTH (IN)		
8	0	0	0		
9	15	0.25	1.14086		
10	30	0.5	2.355945		
11	45	0.75	3.252356		
12	60	1	3.928036		
13	75	1.25	4.438726		
14	90	1.5	4.826142		
15	105	1.75	5.125504		
16	120	2	5.367787		
17	135	2.25	5.580054		
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19	165	2.75	6.000375		
20	180	3	6.238334		
21	195	3.25	6.505373		
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27	285	4.75	8.507161		
28	300	5	8.823376		
29	315	5.25	9.111306		
30	330	5.5	9.366478		
31	345	5.75	9.586911		
32	360	6	10		

=IF(B8<=0,0,IF(B8

Input tabulated depths from TXHYETO.XLS

Time (ddMMMYYYY, HH...	Precipitation (IN)
01Jan2000, 00:00	0
01Jan2000, 00:15	1.140860275
01Jan2000, 00:30	2.355945266
01Jan2000, 00:45	3.2523557
01Jan2000, 01:00	3.92803553
01Jan2000, 01:15	4.438726076
01Jan2000, 01:30	4.826142335
01Jan2000, 01:45	5.125504072
01Jan2000, 02:00	5.367787363
01Jan2000, 02:15	5.580053565
01Jan2000, 02:30	5.785012167
01Jan2000, 02:45	6.000374911
01Jan2000, 03:00	6.238334305
01Jan2000, 03:15	6.5053735
01Jan2000, 03:30	6.802512679
01Jan2000, 03:45	7.126003481

HEC-HMS



Conclusions

- The provisional tool, TXHYETO.XLS, dimensionalizes the Texas dimensionless hyetographs for use in rainfall-runoff models
- Tool uses a distribution-mixture function to approximate the shape of the Texas Dimensionless Hyetograph
- Distribution-mixture model utilized in TXHYETO.XLS replicates estimates made using linear interpolation with a relative error of $<5\%$

References

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- Asquith, W.H., 1998, Depth-duration frequency of precipitation for Texas: U.S. Geological Survey Water-Resources Investigations Report 98–4044, 107 p., <http://pubs.usgs.gov/wri/wri98-4044/> .
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